

MHD SLIP FLOW AND HEAT TRANSFER OVER AN EXPONENTIALLY STRETCHING PERMEABLE SHEET EMBEDDED IN A POROUS MEDIUM WITH HEAT SOURCE

P. R. Sharma^a, Sushila Choudhary^{a,*}, O. D. Makinde^b

^aDepartment of Mathematics, University of Rajasthan, Jaipur-302004, India

^bFaculty of Military Science, Stellenbosch University, South Africa

ABSTRACT

Steady two dimensional laminar magnetohydrodynamic (MHD) slip flow and heat transfer of a viscous incompressible and electrically conducting fluid past over a flat exponentially non-conducting stretching porous sheet embedded in a porous medium with non uniform permeability in the presence of non uniform heat source is investigated. The governing equations of velocity and temperature distributions are solved numerically and the effects of different physical parameters are shown through graphs. The rate of shear stress and the rate of heat transfer at the sheet are derived, discussed numerically and their numerical values for various values of physical parameters are presented through tables.

Keywords: Steady, MHD, stretching sheet, porous medium, heat source, velocity slip, thermal slip, skin friction coefficient and Nusselt number.

1. INTRODUCTION

The study of hydromagnetic electrically conducting fluid flow involving heat transfer over stretching porous sheet is of great importance in many processes as modern metallurgical and metal-working processes. This field has attracted the attention of many researchers because of its possible applications in soil sciences, astrophysics, geophysics, nuclear power reactors etc. In cooling process of nuclear fission reactors, liquid sodium is pumped around using electromagnetic forces. In medical science, an advanced method is used for precisely delivery of medicine to cancer affected organs, in which MHD equations and finite element analysis are used to study the interaction between the magnetic fluid particles in the bloodstream and the external magnetic field. The study of fluid flow through porous medium has become predictable in the extraction of crude oil from the pores of rocks and filtration of solids from liquids. Fluid flow through porous medium also has applications in environment such as flow of ground water through soil and rocks, which is important for agriculture and pollution control. The suction/injection process has its importance in many engineering activities such as in the thermal oil recovery, designing of thrust bearing and radial diffusers. Suction is also applied to chemical processes to remove reactants. In heat pumping technology natural heat sources/sinks like air, ground, water etc. are used. This technology is used in compressors, refrigerators and air conditioners.

Heat transfer of a continuous stretching surface with suction or blowing was analyzed by Chen and Char (1988). Kumaran and Ramanaiah (1996) discussed the flow over a stretching sheet. Heat and mass transfer in the boundary layers on an exponentially stretching continuous surface has been studied by Magyari and Keller (1999). Elbashaeshy (2001) considered heat transfer over an exponentially stretching continuous surface with suction. Slip flow past a stretching surface was investigated by Andersson (2002). Miklavcic and Wang (2006) analyzed viscous flow due to a shrinking sheet. Hydromagnetic flow and heat transfer adjacent to a stretching vertical sheet with

prescribed surface heat flux was studied by Aman and Ishak (2010). Pal and Hiremath (2010) considered computational modeling of heat transfer over an unsteady stretching surface embedded in a porous medium. Boundary layer flow and heat transfer over a stretching sheet with Newtonian heating was studied by Salleh *et al.* (2010). Sharma and Singh (2010) investigated steady MHD natural convection flow with variable electrical conductivity and heat generation along an isothermal vertical plate.

MHD boundary layer flow due to an exponentially stretching sheet with radiation effect was presented by Ishak (2011). Yao *et al.* (2011) studied heat transfer on a generalized stretching/shrinking wall with convective boundary condition. Heat transfer in a fluid through a porous medium over a permeable stretching surface with thermal radiation and variable thermal conductivity was analyzed by Cortell (2012). Hayat (2012) considered three-dimensional flow of a Jeffery fluid over a linearly stretching sheet. Hydromagnetic boundary layer flow over stretching surface with thermal radiation has been discussed by Soid *et al.* (2012). Mandal and Mukhopadhyay (2013) presented heat transfer analysis for fluid flow over an exponentially stretching porous sheet with surface heat flux in porous medium. Slip effects on MHD boundary layer flow over an exponentially stretching sheet with suction/blowing and thermal radiation shown by Mukhopadhyay (2013). Norhafizah *et al.* (2013) studied numerical solution of flow and heat transfer over a stretching sheet with Newtonian heating using the Keller Box Method. Singh and Makinde (2015) presented a similarity solution for the combined effects of velocity slip and temperature jump on boundary layer flow over a moving surface. The MHD slip flow of a conducting Casson nanofluid over a convectively heated stretching sheet was numerically studied by Ibrahim and Makinde (2016a). Other relevant papers with respect to MHD flow over a stretching sheet include Ibrahim and Makinde (2016b); Khan *et al.* (2016).

The aim of the paper is to investigate steady two dimensional laminar MHD flow of a viscous incompressible and electrically conducting fluid past over a flat exponentially non-conducting

*Corresponding author. Email: sumathru11@gmail.com

stretching porous sheet in the presence of non uniform heat source. The governing equations of motion and energy are solved numerically using Runge-Kutta fourth order method along with shooting technique. The effects of the Hartmann number, permeability parameter, Prandtl number, heat source parameter, velocity slip parameter, thermal slip parameter and suction parameter on velocity and temperature distributions are investigated and shown through graphs. The rate of shear stress as skin friction coefficient and the rate of heat transfer as the Nusselt number are derived, discussed numerically and their numerical values for various values of physical parameters are presented through Table 1 and Table 2.

2. MATHEMATICAL FORMULATION OF THE PROBLEM

Steady two dimensional laminar flow of a viscous incompressible and electrically conducting fluid past over a flat exponentially non-conducting stretching porous sheet embedded in a porous medium with non uniform permeability is considered. The x -axis is taken in the direction along the stretching sheet and y -axis is taken normal to it.

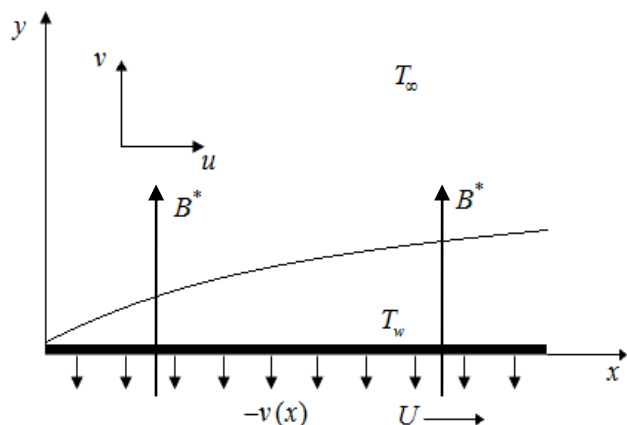


Fig. 1 Physical model and the coordinate system.

The fluid flow confined to $y > 0$. The flow is generated by the action of two equal and opposite forces along the x -axis so that the wall is stretched keeping the origin fixed. The surface is assumed to be highly elastic and is stretched in the x -direction with the velocity

$U = U_0 e^{\frac{x}{l}}$. A non uniform magnetic field $B^* = B_0 e^{\frac{x}{2l}}$ is applied along the y -direction. The magnetic Reynolds is taken to be small and therefore the induced magnetic field is neglected. It is assumed that the

temperature of the sheet T_w is variable and given by $T_w = T_\infty + T_0 e^{\frac{x}{l}}$. A non uniform heat source is also applied. All the fluid properties are assumed to be constant throughout the motion. Under these assumptions, the governing boundary layer equations [Bansal (1977), Bansal (1994), Schlichting and Gersten (2003)] are

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0, \quad (1)$$

$$u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = \nu \frac{\partial^2 u}{\partial y^2} - \left(\frac{\sigma_e B_0^2 l}{\rho} + \frac{\nu}{K^*} \right) u, \quad (2)$$

$$u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} = \frac{\kappa}{\rho C_p} \frac{\partial^2 T}{\partial y^2} + \frac{Q^*}{\rho C_p} (T - T_\infty), \quad (3)$$

where $K^* = K_0 e^{\frac{x}{l}}$ is the non uniform permeability of the medium and $Q^* = Q_0 e^{\frac{x}{l}}$ is the non uniform heat source.

The boundary conditions are

$$y = 0: u = U + L^* \frac{\partial u}{\partial y}, v = -v(x), T = T_w + D^* \frac{\partial T}{\partial y};$$

$$y \rightarrow \infty: u \rightarrow 0, T \rightarrow T_\infty, \quad (4)$$

where $v(x) \left(= V_0 e^{\frac{x}{2l}} \right)$ is the suction velocity at the sheet,

$L^* \left(= L_0 e^{-\frac{x}{2l}} \right)$ is the velocity slip factor and $D^* \left(= D_0 e^{-\frac{x}{2l}} \right)$ is the thermal slip factor.

3. METHOD OF SOLUTION

Introducing the following similarity transformations

$$\eta = y \sqrt{\frac{U_0}{2\nu l}} e^{\frac{x}{2l}}, \theta(\eta) = \frac{T - T_\infty}{T_w - T_\infty}, \psi = \sqrt{2\nu U_0 l} e^{\frac{x}{2l}} f(\eta), \quad (5)$$

The stream function ψ is defined as

$$u = \frac{\partial \psi}{\partial y} \text{ and } v = -\frac{\partial \psi}{\partial x}, \quad (6)$$

which identically satisfies the continuity Eq. (1). Using Eq. (5) into the Eq. (6), we have the velocity components as given below

$$u = U_0 e^{\frac{x}{l}} f'(\eta),$$

$$v = -\sqrt{\frac{\nu U_0}{2l}} e^{\frac{x}{2l}} (\eta f'(\eta) + f(\eta)), \quad (7)$$

where prime denotes the differentiation with respect to η . Now using Eqs. (5) and (7) into the Eqs. (2) and (3), we have

$$f'''' + f f'' - 2 f'^2 - \left(M + \frac{1}{K} \right) f' = 0, \quad (8)$$

$$\theta'' + Pr(f \theta' - \theta f') + 2 Pr Q \theta = 0, \quad (9)$$

where $M \left(= \frac{2\sigma B_0^2 l}{\rho U_0} \right)$ is the Hartmann number, $K \left(= \frac{U_0 K_0}{2\nu l} \right)$ is the

permeability parameter, $Pr \left(= \frac{\mu C_p}{\kappa} \right)$ is the Prandtl number and

$Q \left(= \frac{2Q_0 l}{\rho C_p U_0} \right)$ is the heat source parameter.

The boundary conditions in dimensionless form are reduced to

$$\eta = 0: f = S, f' = 1 + S_v f'', \theta = 1 + S_T \theta';$$

$$\eta \rightarrow \infty: f' \rightarrow 0, \theta \rightarrow 0, \quad (10)$$

where $S \left(= V_0 \sqrt{\frac{2l}{\nu U_0}} \right)$ is the suction parameter, $S_v \left(= L_0 \sqrt{\frac{U_0}{2\nu l}} \right)$ is the

velocity slip parameter and $S_T \left(= D_0 \sqrt{\frac{U_0}{2\nu l}} \right)$ is the thermal slip parameter.

3.1 Coefficient of Skin friction and Nusselt number

Rate of shear stress in terms of coefficient of skin friction at the sheet is given by

$$C_f = \frac{2\tau_w}{\rho U_0^2} = \left(\frac{Re_x}{2} e^{\frac{x}{l}} \right)^{-\frac{1}{2}} f''(0), \quad (11)$$

where τ_w is the wall shear stress given by $\tau_w = \mu \left(\frac{\partial u}{\partial y} \right)_{y=0}$.

Rate of heat transfer in terms of Nusselt number at the sheet is given by

$$Nu = \frac{lq_w}{\kappa(T_w - T_\infty)} = - \left(\frac{Re_x}{2} e^{\frac{x}{l}} \right)^{\frac{1}{2}} \theta'(0), \quad (12)$$

where q_w is the rate of heat transfer given by $q_w = -\kappa \left(\frac{\partial T}{\partial y} \right)_{y=0}$.

4. NUMERICAL SOLUTION

The coupled nonlinear ordinary second order differential Eqs. (8) and (9) along with boundary conditions (10) are solved numerically using MATLAB software. First we convert the boundary value problem into a system of initial value problems as follows:

$$f' = f_1; \quad f_1' = f_2; \quad f_2' = -f f_2 + 2f_1^2 + \left(M + \frac{1}{K} \right) f_1, \quad (13)$$

and

$$\theta' = f_3; \quad f_3' = -Pr(f f_3 - \theta f_1) - 2PrQ\theta. \quad (14)$$

The boundary conditions are

$$f(0) = S, \quad f_1(0) = 1 + S_v f_2(0), \quad \theta(0) = 1 + S_T f_3(0). \quad (15)$$

To solve Eqs. (13) and (14) with boundary conditions (15) as a system of initial value problems we must need the values for $f_2(0)$ i.e. $f''(0)$ and $f_3(0)$ i.e. $\theta'(0)$ but no such values are given. Therefore initial guess values for $f''(0)$ and $\theta'(0)$ are chosen arbitrarily and then we solve the system of initial value problems by using Runge-Kutta fourth order method along with shooting technique. We compare the calculated values of $f'(\eta)$ and $\theta(\eta)$ with the given boundary conditions at $\eta \rightarrow \infty$ i.e. η_∞ . We adjust the values of $f''(0)$ and $\theta'(0)$ to get better approximation of $f'(\eta)$ and $\theta(\eta)$ at η_∞ . In this method, it is necessary to choose a suitable finite value of η_∞ . Here a suitable finite value $\eta_\infty = 2$ is chosen, which depends on the values of the parameters used. In addition the relative error tolerance to 10^{-6} is considered for better convergence.

5. RESULTS AND DISCUSSION

Effects of different physical parameters on velocity and temperature distributions are shown through figures when $M = 0.5, K = 1, Pr = 0.71, Q = 0.5, S = 3, S_v = 0.1$ and $S_T = 0.1$.

Figure 2 shows the effect of permeability parameter on the velocity of the fluid. It is observed that velocity increases with the increment of the permeability parameter. Increment in permeability parameter denotes the increment in the porosity feature of the medium. Clearly, as the porosity of medium is increased, velocity of the fluid through that medium is also increased because fluid got more space with fewer disturbances to flow through medium.

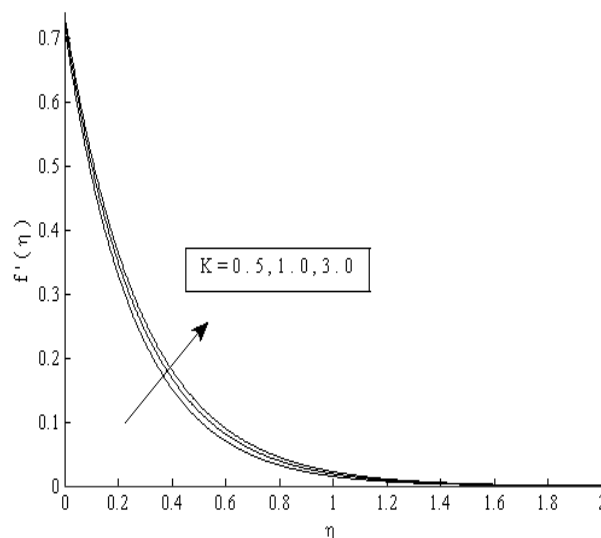


Fig. 2 Velocity distribution for different values of K .

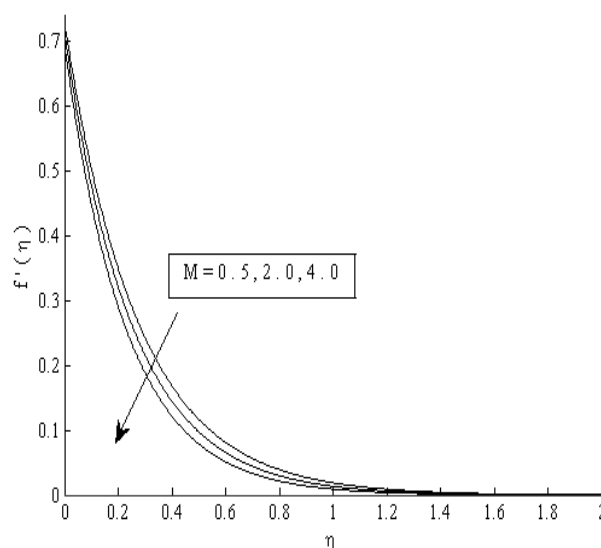


Fig. 3 Velocity distribution for different values of M .

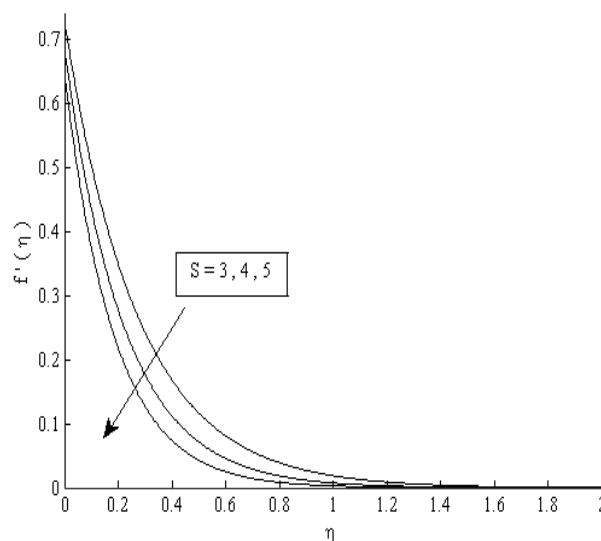


Fig. 4 Velocity distribution for different values of S .

The effect of magnetic parameter (Hartmann number) on velocity of the fluid is displayed in Fig. 3. Due to magnetic field, a resisting force is generated in the flow which is called Lorentz force. This force caused a decline in velocity of the fluid. Therefore as the Hartmann number increases, fluid velocity decreases. It is seen from Fig. 4 that velocity decreases with the increment of suction parameter. Suction parameter shows the porosity of the sheet. As the size of pores of the sheet is increased the flow through the sheet is increased which resist the flow along the sheet. That is the reason of the reduction of fluid flow along the sheet in magnitude.

The effect of velocity slip parameter on fluid velocity is presented in Fig. 5. It is observed that velocity decreases with the increment in the velocity slip parameter. Increment in Hartmann number implies the increment in the strength of Lorentz force. Due to this resisting force, temperature of the fluid is increased. This effect can be observed from Fig. 6. Temperature profile is shown for different values of heat source parameter in Fig. 7. Increment in heat source parameter indicates that external heat is provided to fluid and clearly it causes the enhancement of the fluid temperature. The effect of velocity slip parameter is presented through Fig. 8 and it is observed that fluid temperature increases with the increase of the velocity slip parameter.

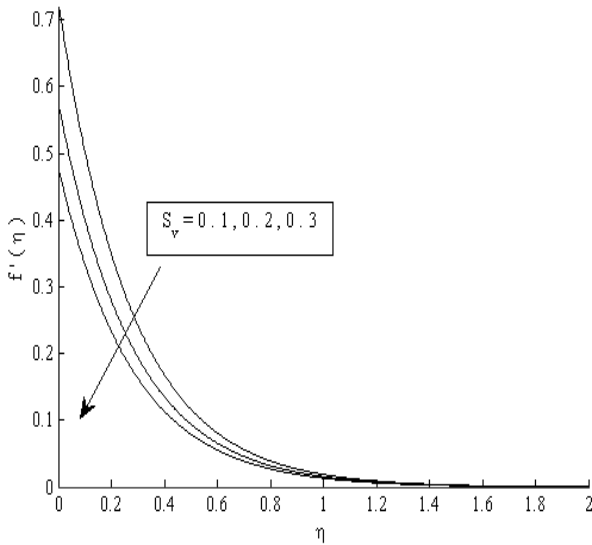


Fig. 5 Velocity distribution for different values of S_v .

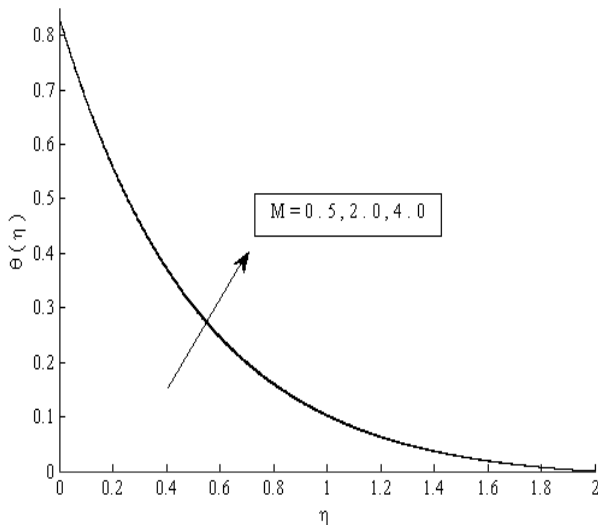


Fig. 6 Temperature distribution for different values of M .

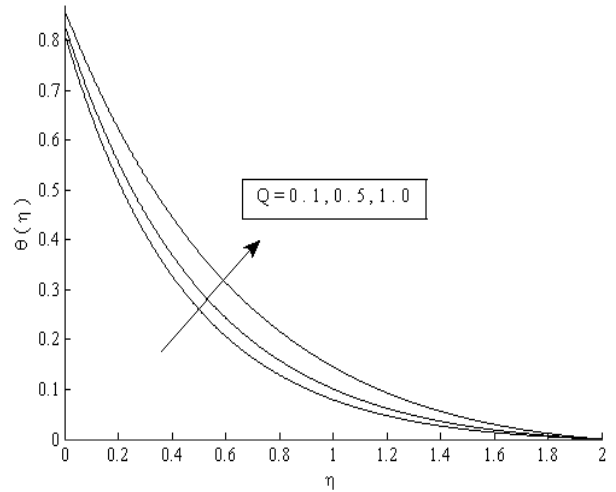


Fig. 7 Temperature distribution for different values of Q .

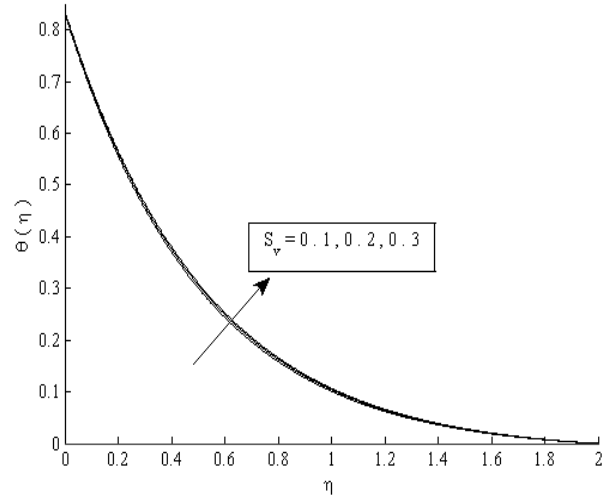


Fig. 8 Temperature distribution for different values of S_v .

Prandtl number is the ratio of momentum diffusivity to thermal diffusivity. Figure 9 shows the effect of Prandtl number on fluid velocity. As the Prandtl number increases thermal conductivity of the fluid decreases, therefore fluid temperature decreases.

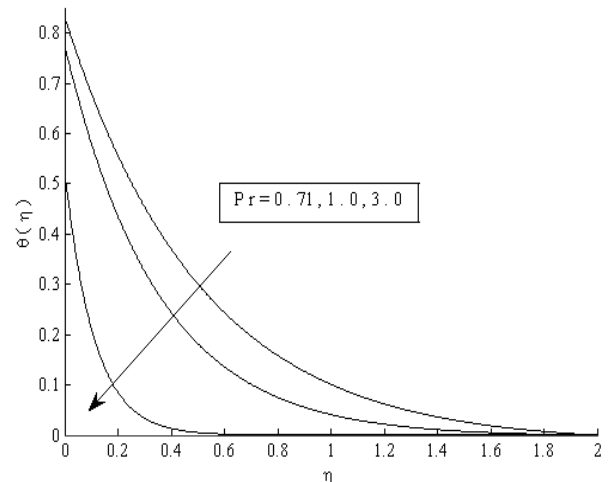


Fig. 9 Temperature distribution for different values of Pr .

Figure 10 shows the effect of suction parameter on fluid temperature and it is observed that fluid temperature decreases with the increase of suction parameter. The effect of thermal slip parameter on fluid temperature is presented in Fig. 11 and it is noted that fluid temperature decreases with the increase of thermal slip parameter.

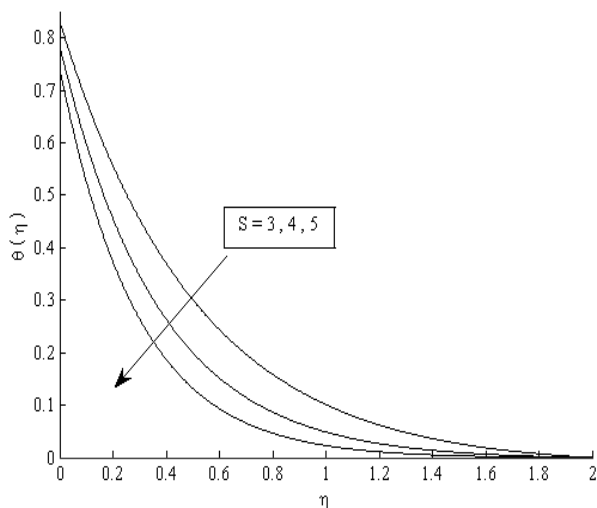


Fig. 10 Temperature distribution for different values of S .

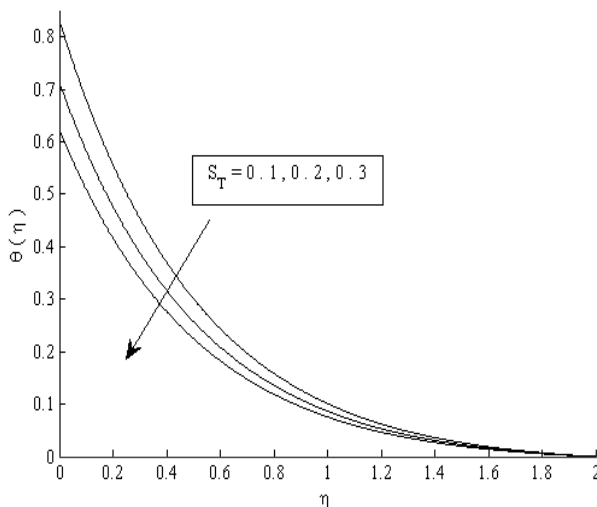


Fig. 11 Temperature distribution for different values of S_T .

Table 1 Numerical values of $f''(0)$ for different values of physical parameters.

K	M	S	S_v	$f''(0)$
1	0.5	3	0.1	-2.7051005
3	0.5	3	0.1	-2.6221080
1	2	3	0.1	-2.8681380
1	0.5	4	0.1	-3.1313106
1	0.5	4	0.3	-1.7351530

It is observed from Table 1 that the skin friction coefficient increases due to increase in the permeability parameter or velocity slip parameter; while it decreases with the increase of the Hartmann number or suction parameter.

Table 2 Numerical values of $-\theta'(0)$ for different values of physical parameters.

K	M	Pr	Q	S	S_v	S_T	$-\theta'(0)$
1	0.5	0.71	0.5	3	0.1	0.1	1.677319
3	0.5	0.71	0.5	3	0.1	0.1	1.682538
1	2	0.71	0.5	3	0.1	0.1	1.667540
1	0.5	1.0	0.5	3	0.1	0.1	2.241582
1	0.5	0.71	1	3	0.1	0.1	1.383828
1	0.5	0.71	0.5	4	0.1	0.1	2.144508
1	0.5	0.71	0.5	3	0.3	0.1	1.632893
1	0.5	0.71	0.5	3	0.1	0.3	1.255982

It is depicted from Table 2 that due to increase of permeable parameter, Prandtl number or suction parameter, the Nusselt number increases; while it decreases with the increase of Hartmann number, heat source parameter, velocity slip parameter or thermal slip parameter.

6. CONCLUSIONS

Steady two dimensional laminar boundary layer flow and heat transfer of a viscous incompressible and electrically conducting fluid past over a flat exponentially non-conducting stretching porous sheet in the presence of non uniform transverse magnetic field and non uniform heat source are analyzed numerically. Effect of different physical parameters on fluid velocity, fluid temperature, skin friction coefficient and Nusselt number are investigated and the following observations are made:

- As the Hartmann number increases, the fluid velocity decreases; whereas the fluid temperature increases.
- An increase in heat source parameter results an increase in the fluid temperature
- The fluid velocity and fluid temperature decrease with the suction parameter.
- As the velocity slip parameter increases, the fluid velocity decreases, while opposite behavior is seen for fluid temperature.
- The fluid temperature increases with the increase of heat source parameter; while it decreases with the Prandtl number.
- The skin friction coefficient and the Nusselt number increase due to increase in the permeability parameter.
- Due to increase of Prandtl number, Nusselt number increases; while Nusselt number decreases with the increase of heat source parameter.

NOMENCLATURES

B_0	Constant magnetic field intensity, kg/s^2A
C_f	Skin friction coefficient
C_p	Specific heat at constant pressure, J/kgK
D_0	Initial value of thermal slip factor, m
f	Dimensionless stream function
K_0	Initial permeability of the medium, m^2
L_0	Initial value of velocity slip factor, m
q_w	Heat flux, W/m^2
Q_0	Constant initial heat source, J/m^3sK
Re_x	Local Reynolds number
Nu	Nusselt number

T	Fluid temperature within the boundary layer, K
T_0	Temperature increase along the sheet, K
T_w	Temperature of the sheet, K
T_∞	Temperature far away from the sheet, K
U	Stretching velocity, m/s
U_0	Reference velocity, m/s
U_∞	Free stream velocity, m/s
V_0	Initial strength of suction, m/s
l	Reference length, m
u	Dimensionless velocity in x direction, m/s
v	Dimensionless velocity in y direction, m/s
x, y	Axial and transverse co-ordinates, m

Greek Symbols

η	Similarity variable
θ	Dimensionless temperature
κ	Thermal conductivity, W/mK
μ	Viscosity, $Kg/m s$
ν	Kinematic viscosity, m^2/s
ρ	Density, Kg/m^3
σ_e	Electric conductivity
ψ	Stream function

Abbreviations

MHD	Magnetohydrodynamics
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