

Reducing PM Eddy Current Rotor Losses by Partial Magnet and Rotor Yoke Segmentation

Dominic A. Wills, Maarten J. Kamper

Abstract -- In order to reduce the losses caused by eddy currents in the magnets and rotor yoke of a PM electric machine, a number of effective methods can be used. One method that imposes the least restrictions on machine performance is segmentation, which can be difficult to implement as magnets need to be cut, insulated and re-glued, which is a laborious and costly process. This paper presents methods of partial segmentation in magnets and the rotor yoke that aim to improve machine performance by reducing eddy current loss, while also suggesting realistic manufacturing possibilities. Results are obtained using analytical, numerical and experimental methods and good agreement is achieved.

Index Terms— permanent magnet, eddy current, losses, partial segmentation, rotor yoke, analytical, finite element.

I. INTRODUCTION

Eddy currents flowing in the rotor of a permanent magnet synchronous machine (PMSM) can be detrimental to a machine's performance. The ohmic power loss caused by circulating eddy currents is a source of inefficiency, and the heat produced in a solid rotor yoke can raise the magnet temperature above its recommended operating range causing partial, irreversible demagnetization.

In principle, a high proportion of eddy currents in the rotor are induced by asynchronously rotating stator MMF harmonics found with certain types of PMSM machine topologies. Methods to protect the rotor from the harmonics include closing the stator winding slots, including a steel retaining ring over the magnets, enlarging the air gap and segmenting the solid conducting regions.

A segmented region is comprised of smaller, insulated material pieces. Segmentation is the preferred method for reducing rotor losses as it has the least influence on the machine's performance. In this study, we consider the magnet and rotor regions to be radially segmented, i.e.: the incisions are made down the machine's axial length, as shown in Fig. 1. It has been shown that magnet segmentation has a marked effect on reducing eddy current magnet losses [1-3, 9-11,14]. Using analytical methods, these studies show the strong relationship between increased segmentation and reduction in magnet eddy current losses.

In [1], the author uses the stator current time harmonics to predict an inverse square relationship between the width of the magnet and the reduction in losses. In [4], [5] the model is expanded to include the moving MMF spatial harmonics in the stator winding. In [3], the model is extended to also include the reaction fields of the induced currents in the magnets and the yoke. The results of these methods agree that increased levels of segmentation lead to significantly lower magnet eddy current losses.

The segmentation manufacturing process includes cutting the magnet into equal-sized pieces after which the 'segments' are glued back together. This manufacturing process can prove to be costly and labour intensive, which prompts some manufacturers to avoid segmentation and find alternative means to reduce magnet losses. This study presents two alternative methods to full magnet segmentation (FMS) which aim to address some of the construction difficulties with FMS while still providing a considerable saving in rotor losses. Assumptions include ignoring the eddy current end effects as this model is computed in 2-D only.

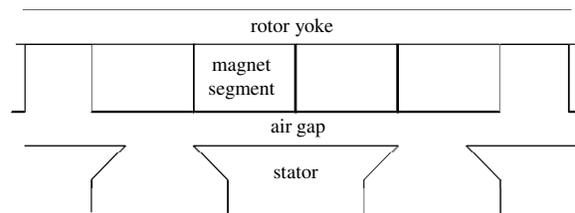


Fig. 1: A machine cross-section showing full magnet segmentation.

II. ROTOR LOSS MODEL

For the machine model, a radial flux PMSM machine is unrolled to create a linear machine model in the (x,y,z) plane shown in Fig. 2. The co-ordinate axes are fixed to the moving rotor reference frame. A current sheet lies on the stator surface and represents either a balanced three phase stator winding flowing in the z direction or a collection of harmonics present due to the effect of slotting or a combination of both. The definitions of these current sheets can be found in [2] for the case of the three phase winding or in [6] for the case of stator slotting. In this study, for accuracy, the harmonic magnitudes are extracted from a single time step finite element solution on the stator surface and are represented as:

$$H_{(\mu)}(x_s, t) = \sum_{\mu=1}^{\infty} h_{(\mu)} \cos(\omega t - \pi \mu x_s), \quad (1)$$

$$H_{(\mu)}(x, y, t) = \sum_{\mu=0}^{\infty} \sum_{i=1,3,5,\dots}^{\infty} \frac{\Lambda_{\mu}(y) B_{rem}}{2 \left(\mu N_s \pm i \frac{N_p}{2} \right)} \cdot \cos \left[\left(\mu N_s \pm i \frac{N_p}{2} \right) x_r + \mu N_s \omega_s t \right] \quad (2)$$

for the current harmonics and slotting harmonics respectively, where μ is the spatial harmonic, $h_{(\mu)}$ is the magnitude of the μ^{th} spatial harmonic, ω is the angular frequency of the μ^{th} harmonic, ω_s is the synchronous rotor angular velocity, x_s is the stator x variable, x_r is the rotor reference frame x variable, N_s is the number of slots, N_p is the number of poles, B_{rem} is the flux density for a uniform air gap, $\Lambda(y)$ is the permeance variation due to slotting and t is time. The higher order time harmonics are ignored as we assume purely sinusoidal stator current waveforms.

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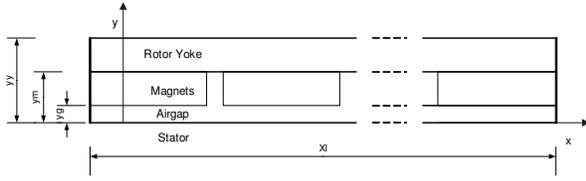


Fig. 2: The linear machine model shown in the x,y plane.

The machine is divided into regions which describe the rotor yoke, magnets, air gap and stator as seen in Fig. 2. Each region has different properties of permeability and conductivity, leading to different solution constants for the magnetic vector potential function in each.

The transfer function to convert the stationary stator current loading harmonics onto the rotating rotor reference frame is defined as

$$\omega = \omega_s - 2\pi n, \quad (3)$$

where n is the rotor speed. Note that when μ is equal to the torque-producing working harmonic, the speed of this harmonic relative to the rotor is zero as the two harmonics are rotating synchronously in the air gap. All other current loading harmonics rotate asynchronously in the rotor causing eddy currents in the magnets and rotor yoke. In order to determine the eddy current function in the magnets, the magnetic vector potential, A is used. We use Poisson's Equation to solve for A ,

$$\nabla^2 A - j\omega\kappa\mu A = 0 \quad (4)$$

Using the method of separation of variables, which assumes that the overall function can be written as a product of two functions of x and y respectively, we assume the form:

$$A(x, y) = A(x)A(y) \quad (5)$$

This gives Poisson's Equation in the form of

$$\frac{d^2 A(x)}{dx^2} \cdot \frac{1}{A(x)} + \frac{d^2 A(y)}{dy^2} \cdot \frac{1}{A(y)} = 0 \quad (6)$$

Various solutions are available for this differential equation. Ignoring eddy currents, the solution best fitting this model is:

$$A(x, y) = (C_y e^{\gamma y} + D_y e^{-\gamma y}) e^{-\alpha x} \quad (7)$$

where $\gamma^2 = \alpha^2 + j\omega\kappa\mu$, and $\alpha = \mu\pi$ (8)

The general solution for the magnetic vector potential in each region is shown in (7). The next step is to define the exact constants for each region, which is done by defining the boundary conditions at the edges of the three regions studied. There are two conditions to be applied at the boundaries of each region:

$$B_{n,k} = B_{n,k+1} \quad (9)$$

$$H_{t,k+1} - H_{t,k} = A_k \quad (10)$$

The boundary conditions stipulate that the normal value of flux density should be continuous across regions and that changes in tangential field intensity are created by the presence of current loading. The stator surface vector potential is defined by the stator loading current sheet. The air gap, magnets and yoke interfaces have continuous normal flux and have zero current loading, and the vector potential of the outer yoke boundary is set to zero. The detailed calculation of these constants can be found in [3]. One now has the complete, analytical solution for the magnetic vector potential in the areas of interest in the rotor of the machine. The particular quantity of interest for calculation of ohmic loss in the magnets is the eddy current density. The direction of the eddy current is assumed to be in the z-direction only and is calculated by:

$$J(x, y) = -j\omega A(x, y) + \text{grad}\Phi \quad (11)$$

where Φ is a constant in the (x,y) plane. The eddy currents flowing in a solid conductor must have an equal and opposite return path i.e. taking the direction into account, currents in a conductor must sum to zero. The constant $\text{grad}\Phi$ term is used to offset residual DC current. Thus, we have:

$$J_{seg}(x, y) =$$

$$\sum_{i=0}^{Np-1} \sum_{k=0}^{Nss-1} J(x, y) \int_0^{h_m} \int_{\frac{2\pi i}{Np} + \frac{\tau(k+1)}{Nss}}^{\frac{2\pi i}{Np} + \frac{\tau k}{Nss}} J(x, y) dx dy \quad (12)$$

It should be noted at this juncture, that the change in current density due to the post process condition imposed in (12) will affect the field solution calculated from (9). This possible effect is ignored in the analytical calculations, but is taken into account in the FE analysis through the setting up of boundary conditions. The total power is calculated as:

$$P_{ave} = \frac{l_m}{2\sigma} J_{seg}(x, y) \cdot J_{seg}(x, y)^* \quad (13)$$

A. Partial Magnet Segmentation

The first proposed method to reduce the magnet loss is shown in Fig. 3(a) called *single-sided partial magnet segmentation* (SS-PMS). This technique is similar to full segmentation; however the penetration of the incision is less than 100%. This technique ensures that the magnet stays in one piece during manufacture, which avoids complications with trying to bond fragmented magnet pieces. The second alternative shown in Fig. 3(b) is called *double-sided partial magnet segmentation* (DS-PMS). This technique uses the concept of SS-PMS, except that non-aligned cuts are made from either face of the magnet. This method also ensures that the magnet stays in one piece during the process of segmentation, but the advantage is that both sides of the magnet are segmented. These two techniques of PMS seek to alleviate some of the construction challenges experienced with FMS, while still aiming to achieve good eddy current loss reduction. The extent to which these loss reduction benefits are realized, forms the subject of this study.

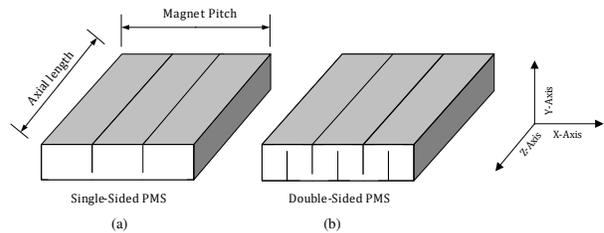


Fig. 3: Cross sections of (a) single-sided and (b) double-sided partially segmented magnets, showing incisions having partial penetration only.

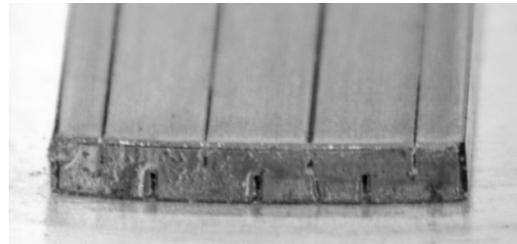


Fig. 4: Double-sided partially segmented magnet with incisions cut from both sides of the magnet and 50% penetration.

B. Partial Rotor Yoke Segmentation

When voltages are induced in a solid conductor due to magnetic flux pulsations, the induced eddy current magnitudes are determined by the resistivity and the geometric dimensions of the solid in which they flow. In order to reduce losses in a solid rotor yoke, one must find a way to increase the resistivity without changing the material. This section describes a method of increasing the resistivity ‘seen’ by the eddy currents called *partial rotor yoke segmentation* (PRYS).

PRYS is a technique where the solid yoke is finely cut along the surface adjacent to the magnets as shown in Fig. 5. The aim of the cut is to create isolated conducting regions interrupting the eddy current flow. The depth of the cut is called the segmentation penetration depth and an optimum value depends on the conductivity, permeability, and the wavelength of the destructive field harmonics in the rotor. In many cases a segmentation penetration depth value much less than the thickness of the yoke can be selected.

The model used in this work is an analytical model of the stator MMF harmonics in the machine. The model includes the effect of the eddy current reaction field; however it neglects the effect of non-linear saturation properties of the steel rotor yoke. What is aimed for is a good machine model that can give insight and understanding into the causes of the magnet loss to help guide the design process. Finite element (FE) analysis is used for accurate prediction of results and comparison.

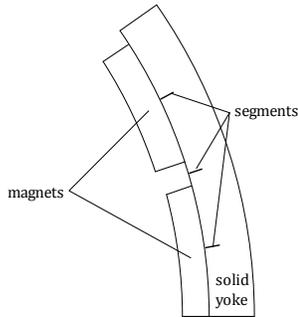


Fig. 5: Solid yoke partial segments positioned on the magnet side of the solid rotor yoke.

III. RESULTS

In order to make a definitive comparison of the methods of partial segmentation, three methods of generating results were used. The analytical model was used to gain qualitative results and understanding, the FE method was used to gain accurate results especially when materials with non-linear properties are used. A test machine was also built with a variety of rotors in order to validate the results obtained. The machine used was an outer rotor, 40 pole, 48 slot, non-overlap, single layer wound, 15kW PM machine seen in Fig. 6, with its machine data shown in Table I.

To ensure consistency in the analytical model, FEA results are used to define the stator surface current sheet. The magnitude of each field harmonic is extracted from the stator surface FE calculation using a Fourier transformation, and eddy currents are computed using the harmonic magnitude and frequency. This frequency is calculated using Table II. The model was used to calculate the eddy currents in the magnet in order to compute the total magnet loss which was used to compare the novel proposed methods of partial segmentation.

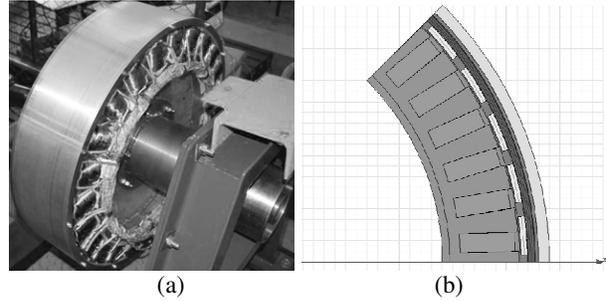


Fig. 6: (a) PM test machine and (b) layout of FE machine model.

A. Single-sided Partial Magnet Segmentation

The cross sectional power density function in the magnet is shown in Fig. 7 for varying degrees of SS-PMS. The segmented portion of the magnet has a marked effect on the magnet loss density in that region, while the unsegmented portion of the magnet predictably returns a loss profile expected in a solid magnet. It is clear from the power density function in Fig. 7 that when considering SS-PMS, segmentation in the air gap-facing half of the magnet is most effective as this targets the half of the magnet with the higher power density. The overall loss improvement with SS-PMS calculated numerically and analytically is shown in Fig. 8.

B. Double-sided Partial Magnet Segmentation

The power loss density benefit associated with using DS-PMS is shown in Fig. 9. To avoid alignment of the magnet segments, the front and back of the magnet have differing degrees of segmentation, which explains the small discontinuity in magnet loss density appearing halfway through the magnet. This unequal segmentation underpins the reason why DS-PMS marginally outperforms the FMS. The relationship between magnet loss and segmentation is shown in Fig. 10 for a magnet with DS-PMS. It is clear that there is a significant reduction in magnet loss with increasing level of segmentation. The comparison of DS-PMS with FMS can be further seen in Fig. 11, where they achieve very similar loss reduction properties with increasing segmentation.

TABLE I

MACHINE DIMENSIONS AND PHOTOGRAPH OF THE PERMANENT MAGNET SYNCHRONOUS MACHINE THAT WAS USED FOR TESTING AND ANALYSIS.

Machine Parameter	Dimension
Stator inner diameter	247 mm
Stator outer diameter	311.5 mm
Rotor outer diameter	326.75 mm
Stack length	100 mm
Rotor yoke thickness	7.25 mm
Magnet pitch	0.73%
Magnet thickness	6 mm
Rated speed	150 rpm
Air gap length	2 mm
Coil width	18 mm
Tooth width	11.1 mm

TABLE II

THE TABLE DESCRIBES FIELD HARMONIC ORIGIN AND SHOWS THE HARMONIC FREQUENCY CALCULATION.

Harmonic source	Harmonic Definition	Harmonic frequency relative to rotor
Stator winding	$\mu = n \cdot scm(N_p, N_s)$ $n = 1, 5, 7, 11, 13 \dots$	$\omega = \frac{2\pi n_s}{60} \left(\frac{N_p}{2} - \mu \right)$
Static Magnet	$\mu = \frac{n \cdot N_p}{2}$ $n = 1, 3, 5 \dots$	$\omega = 0$
Slotting	$\mu = n N_s + i \frac{N_p}{2}$ $n = 1, 2, 3 \dots$ $i = \pm 1, 3, 5 \dots$	$\omega = \frac{i}{abs(i)} \frac{2\pi n_s N_s R_s}{60}$

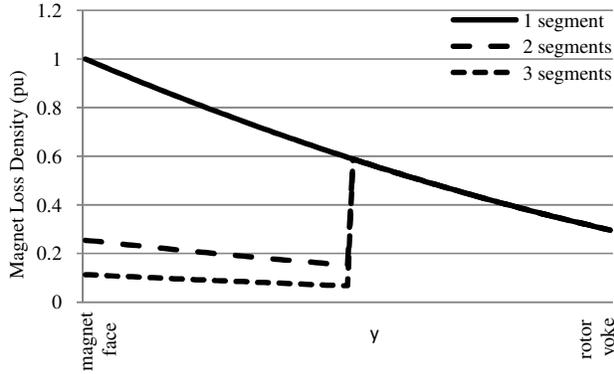


Fig. 7: Magnet loss change from the magnet face to the rotor yoke in a magnet with SS-PMS and 50% penetration.

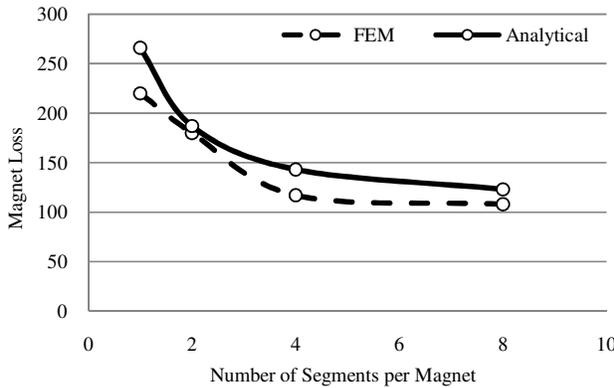


Fig. 8: Analytical and FE calculated magnet loss versus number of magnet segments with SS-PMS.

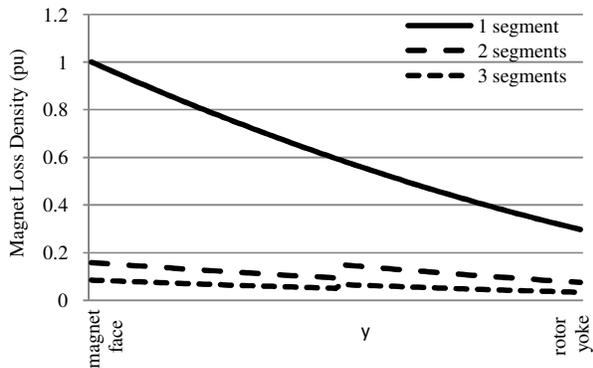


Fig. 9: Magnet loss change from the magnet face to the rotor yoke in a magnet with DS-PMS and 50% penetration.

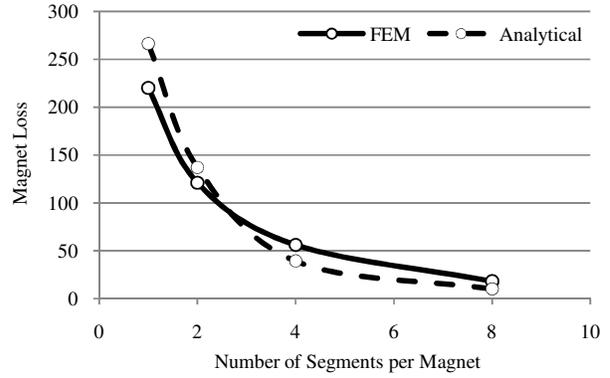


Fig. 10: Analytical and FE calculated magnet loss versus number of magnet segments with DS-PMS.

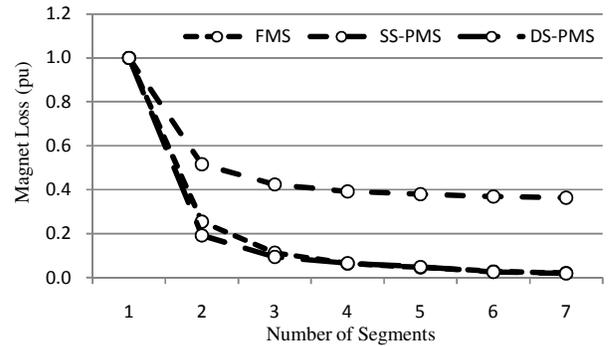


Fig. 11: Analytically calculated magnet loss versus number of segments for the three methods of magnet segmentation.

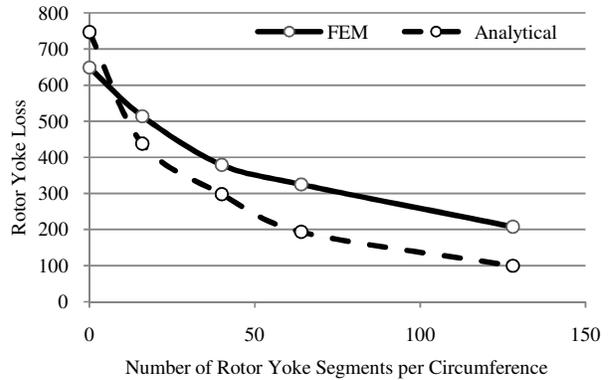


Fig. 12: Analytical and FE calculated rotor yoke loss versus level of rotor yoke partial segmentation and 17.5% penetration.

C. Partial Rotor Yoke Segmentation

The effect of the number of partial rotor yoke segments in minimizing the rotor yoke solid loss is shown in Fig. 12. The agreement between the analytical and FE method results is slightly compromised by the effect of varying permeability in the steel. Nevertheless, a good performance return is at higher levels of segmentation. Including 128 incisions around the inner yoke diameter of the machine with a penetration of 17.5% of the 7.25mm yoke thickness shows a solid loss reduction (FE calculated) of 68% in the yoke. Using the calculation method in the Appendix, this improvement translates into a 24.8°C reduction in the yoke temperature and an overall efficiency improvement of 2.94%.

The power density graph in Fig. 13 shows the intensity of the power loss due to eddy current flow in the cross section of

the rotor yoke calculated analytically. It is clear in this study that due to the skin effect in the steel, the eddy currents only flow within $\pm 30\%$ of the steel closest to the magnet interface. Thus, it is not necessary to segment the rotor yoke with a penetration greater than this percentage.

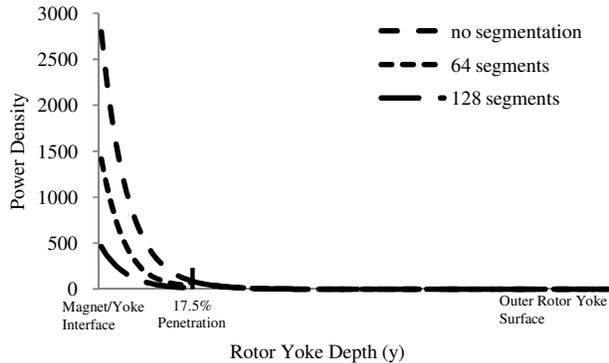


Fig. 13: Power density in the rotor yoke due to eddy currents flow.

D. Comparison with measured results

The magnet eddy current losses are measured using a technique described in the Appendix. The losses are measured from the machine in Fig. 6a that was built with two separate rotors to test the effect of DS-PMS. The first rotor contained solid magnets while the second rotor contained DS-PMS magnets with four segments per magnet as shown in Fig. 4. The test machine is operated in generator mode with no electrical load as this eliminates the copper loss in the machine and also much of the stator core loss. TABLE III gives a comparison between the total rotor loss in the two rotors as measured and as calculated using analytical and FE methods. The loss improvement column shows the performance benefit of introducing DS-PMS over using solid magnets.

TABLE III

TOTAL ROTOR POWER LOSS OF THE TEST MACHINE AT 150R/MIN AT NO LOAD WITH SOLID AND DS-PMS MAGNETS.

	Solid Magnets (W)	DS-PMS Magnets (W)	Loss Improvement (W)
FEM	755	591	164
Analytical	781	554	227
Measured	807	607	200

E. Overall Comparison

The main FE calculated results of the test machine at full load are given in Table IV, i.e. to compare the various loss reduction techniques side-by-side. There can be confidence of their accuracy given the close agreement of measured and FE calculated results. These techniques include single and double sided partial magnet segmentation and partial rotor yoke segmentation.

If the best case scenario is extracted from Table IV, it can be deduced that implementation of DS-PMS with four segments per magnet and coupled with PRYS with 128 segments, would yield an efficiency improvement of 4.1% and a temperature reduction of 34.7°C; which would have the PM rotor running at approximately 75°C at full load, which is well within the operating temperature range of the magnets.

TABLE IV

EFFECT OF VARIOUS LOSS REDUCTION TECHNIQUES ON THE FULL LOAD FE CALCULATED ROTOR EDDY CURRENT LOSSES OF THE TEST MACHINE.

Technique	Number of Segments	Magnet/yoke Loss (W)	% Loss Reduction	Temperature Reduction (°C)
SS-PMS (per magnet)	1	229	0	0
	4	138	39.7	5.11
	8	118	48.4	6.23
DS-PMS (per magnet)	1	229	0	0
	4	53	76.9	9.88
	8	32	86	11
PRYS (per circumference)	1	649	0	0
	64	325	50	18.2
	128	208	68	24.8

IV. CONCLUSION

It is clear from analytical calculations that the rotor eddy current density decays exponentially with distance from the stator surface in both the magnets and the rotor yoke. SS-PMS makes use of this property by implementing segmentation only on the stator-facing half of the magnet where the losses are more concentrated. Given the relative ease with which SS-PMS can be implemented and the low extra cost incurred, the price to performance ratio makes SS-PMS a very attractive option. DS-PMS shows that even a relatively low level of segmentation can realize a significant reduction in losses. It can be concluded that DS-PMS is at least as effective as FMS at reducing magnet losses, while also being considerably easier to implement.

The exponential decay of the current density can be seen more clearly demonstrated in the rotor yoke due to the higher conductivity and permeability values. The rotor yoke eddy current density of the tested machine is shown to vanish completely within the first 30% of the yoke from the stator-facing side. This phenomenon explains the success of partial rotor yoke segmentation, as only the eddy current conducting area of the yoke needs to be segmented. This is quite achievable with minimal sacrifice in machine performance.

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VI. BIOGRAPHIES

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VII. APPENDIX

The no load rotor loss measurement is done by comparing the losses in three different PM rotors. The rotors are identical in geometry, but differ in terms of magnet segmentation and rotor yoke core material as:

- PM rotor 1: solid magnets and solid mild steel rotor yoke;
- PM rotor 2: DS-PMS and solid mild steel rotor yoke;
- PM rotor 3: DS-PMS and laminated rotor yoke.

For each of the three PM rotors the input shaft power, $P_{in} = \omega_s \tau$, and the steady state outer rotor temperature, T_{ro} , are measured, with the PM machine each time at no load and driven at a speed of 150 r/min. Assuming no hysteresis loss in the PM rotor, the first equation for the total rotor eddy current loss, P_{er} , is given by

$$P_{er} = P_{in} - P_{loss}, \quad (14)$$

where $P_{loss} = P_{wf} + P_s$, i.e. equal to the wind and friction losses plus the core and winding eddy current losses in the stator.

In a second equation for P_{er} Newton's thermal law of cooling is considered. In the thermal model two assumptions are made. Firstly it is assumed that heat transfer takes place only through convection, thus heat transfer through radiation is ignored. Secondly, heat transfer to ambient via moving air in the air gap is ignored. With these two assumptions P_{er} can be expressed approximately as

$$P_{er} = \frac{dQ}{dt}, \quad (15)$$

$$\approx h_o A_o (T_{ro} - T_a) + h_i A_i (T_{ri} - T_{as})$$

where Q is the heat energy, h_o and h_i are the outer and inner rotor surface heat transfer coefficients, A_o and A_i are the outer and inner rotor yoke surface areas, T_{ro} and T_{ri} are the measured outer and inner rotor surface temperatures and T_a and T_s are the ambient and stator temperatures respectively. It was found during measurements that $T_s \approx T_a$ and that $T_{ri} \approx T_{ro}$, so that (15) can be simplified as

$$P_{er} \approx (h_o A_o + h_i A_i) (T_{ro} - T_a), \quad (16)$$

$$= h A (T_{ro} - T_a)$$

From (14) and (16) three equations can be obtained for the three PM rotor measurements assuming P_{loss} stays constant, namely as

$$P_{in(1)} - P_{loss} \approx h A (T_{ro} - T_a)_1$$

$$P_{in(2)} - P_{loss} \approx h A (T_{ro} - T_a)_2, \quad (17)$$

$$P_{in(3)} - P_{loss} \approx h A (T_{ro} - T_a)_3$$

where subscripts 1, 2 and 3 refer to PM rotor 1, PM rotor 2 and PM rotor 3 respectively as described above. From (17) on average the constants P_{loss} and hA can be determined. With these constants known P_{er} can be determined by (14) or (16). Obviously, from (17) the power loss difference DS-PMS makes can also be measured.